

Hong Kong Mathematics Olympiad (1993 – 94)

Final Event – Sample (Individual)

香港数学竞赛 (1993 – 94)

决赛项目 – 样本 (个人)

- (i) The sum of two numbers is 40, their product is 20. If the sum of their reciprocals is  $a$ , find  $a$ .

$a =$

某两数之和为 40，其积为 20。若该两数倒数之和为  $a$ ，求  $a$ 。

- (ii) If  $b \text{ cm}^2$  is the total surface area of a cube of side  $(a+1) \text{ cm}$ , find  $b$ .

$b =$

若一边长  $(a+1)$  厘米之正方体之总表面积为  $b$  平方厘米，求  $b$ 。

- (iii) One ball is taken at random from a bag containing  $(b-4)$  white balls and  $(b+46)$  red balls. If  $\frac{c}{6}$  is the probability that the ball is white, find  $c$ .

$c =$

一袋内有  $(b-4)$  个白球， $(b+46)$  个红球。若随意于袋内取一球，而该球为白色之概率为  $\frac{c}{6}$ ，求  $c$ 。

- (iv) The length of a side of an equilateral triangle is  $c \text{ cm}$ . If its area is  $d\sqrt{3} \text{ cm}^2$ , find  $d$ .

$d =$

若一边长  $c$  厘米之正三角形之面积  $d\sqrt{3}$  平方厘米，求  $d$ 。

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Final Event 1 (Individual)

香港数学竞赛 (1993 – 94)

决赛项目 1 (个人)

- (i) The equation  $x^2 - ax + (a + 3) = 0$  has equal roots. Find  $a$ , if  $a$  is a positive integer.

$a =$

方程式  $x^2 - ax + (a + 3) = 0$  有等根。若  $a$  为一正整数，求  $a$ 。

- (ii) In a test, there are 20 questions.  $a$  marks will be given to a correct answer and 3 marks will be deducted for each wrong answer. A student has done all the 20 questions and scored 48 marks. Find  $b$ , the number of questions that he has answered correctly.

$b =$

在一次测验中，共 20 题。做对一题给  $a$  分，做错一题要倒扣 3 分。一学生做了全部的 20 题，而得到 48 分。他答对了的题目数目是  $b$ 。求  $b$ 。

- (iii) If  
若

$$x : y = 2 : 3$$

$$x : z = 4 : 5$$

$$y : z = b : c,$$

find  $c$ .

求  $c$ 。

$c =$

- (iv) Let  $P(x, d)$  be a point on the straight line  $x + y = 22$  such that the slope of  $OP$  equals to  $c$  ( $O$  is the origin). Determine  $d$ .

$d =$

设  $P(x, d)$  为直线  $x + y = 22$  上的点，且  $OP$  的斜率为  $c$  ( $O$  为原点)。求  $d$ 。

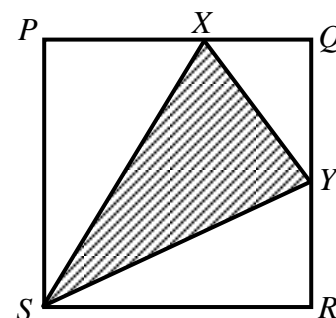
Hong Kong Mathematics Olympiad (1993 – 94)

Final Event 2 (Individual)

香港数学竞赛 (1993 – 94)

决赛项目 2 (个人)

- (i) In square  $PQRS$ ,  $Y$  is the mid-point of the side  $QR$  and  $PX = \frac{3}{4}PQ$ . If  $A$  is the ratio of the area of the shaded triangle to the area of the square, find  $A$ .



在正方形  $PQRS$  中,  $Y$  为  $QR$  之中点, 且  $PX = \frac{3}{4}PQ$ 。若  $A$  为阴影部分三角形面积与正方形面积的比, 求  $A$ 。

$A =$

- (ii) A man bought a number of ping-pong balls where a  $16A\%$  sales tax is added. If he did not have to pay tax he could have bought 3 more balls for the same amount of money. If  $B$  is the total number of balls that he bought, find  $B$ .

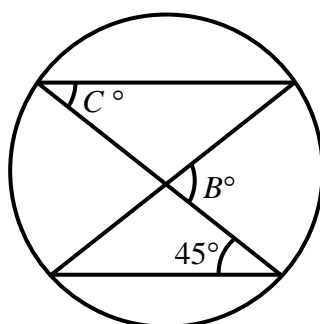
$B =$

某甲买了一些乒乓球, 需多付出销售税  $16A\%$ 。若他毋须付税, 则可用同等金钱多买 3 个乒乓球。假设  $B$  是他所买乒乓球的个数, 求  $B$ 。

- (iii) Refer to the diagram, find  $C$ .

$C =$

如图, 求  $C$ 。



- (iv) The sum of  $2C$  consecutive even numbers is 1170. If  $D$  is the largest of them, find  $D$ .

$D =$

$2C$  个连续偶数之和为 1170。若  $D$  为其中最大之偶数, 求  $D$ 。

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Final Event 3 (Individual)

香港数学竞赛 (1993 – 94)

决赛项目 3 (个人)

- (i) If  $183a8$  is a multiple of 287, find  $a$ .

$a =$

若  $183a8$  为 287 的倍数，求  $a$ 。

- (ii) The number of factors of  $a^2$  is  $b$ , find  $b$ .

$b =$

$a^2$  这个数共有  $b$  个因子，求  $b$ 。

- (iii) In an urn, there are  $c$  balls,  $b$  of them are either black or red,  $(b+2)$  of them are either red or white and 12 of them are either black or white. Find  $c$ .

$c =$

瓶中有球  $c$  个，其中  $b$  个是黑色或红色的， $(b+2)$  个是红色或白色的，而黑色或白色的有 12 个。求  $c$ 。

- (iv) Given  $f(3+x) = f(3-x)$  for all values of  $x$ , and the equation  $f(x) = 0$  has exactly  $c$  distinct roots. Find  $d$ , the sum of these roots.

$d =$

已知对所有  $x$ ， $f(3+x) = f(3-x)$ ，且方程式  $f(x) = 0$  有  $c$  个不等根，求所有根的总和  $d$ 。

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Final Event 4 (Individual)

香港数学竞赛 (1993 – 94)

决赛项目 4 (个人)

- (i) The remainder when  $x^6 - 8x^3 + 6$  is divided by  $(x-1)(x-2)$  is  $7x - a$ , find  $a$ .

$a =$

$x^6 - 8x^3 + 6$  除以  $(x-1)(x-2)$ , 其余数为  $7x - a$ , 求  $a$ 。

- (ii) If  $x^2 - x + 1 = 0$  and  $b = x^3 - 3x^2 + 3x + a$ , find  $b$ .

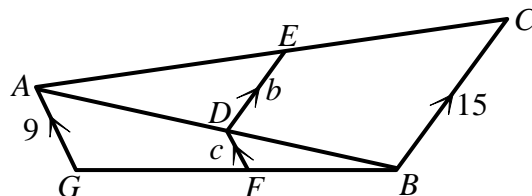
$b =$

若  $x^2 - x + 1 = 0$  及  $b = x^3 - 3x^2 + 3x + a$ , 求  $b$ 。

- (iii) Refer to the diagram, find  $c$ .

$c =$

如图, 求  $c$ 。



- (iv) If  $c$  boys were all born in June 1990 and the probability that their birthdays are all different is  $\frac{d}{225}$ , find  $d$ .

$d =$

有  $c$  个儿童, 他们均生于一九九零年六月, 若果他们生于不同日子的概率是  $\frac{d}{225}$ , 求  $d$ 。

**Hong Kong Mathematics Olympiad (1993 – 94)**

**Final Event 5 (Individual)**

**香港数学竞赛 (1993 – 94)**

**决赛项目 5 (个人)**

- (i) Given  $1 - \frac{4}{x} + \frac{4}{x^2} = 0$ . If  $A = \frac{2}{x}$ , find  $A$ .

$A =$

已知  $1 - \frac{4}{x} + \frac{4}{x^2} = 0$ 。若  $A = \frac{2}{x}$ ，求  $A$ 。

- (ii) If  $B$  circular pipes each with an internal diameter of  $A$  cm carry the same amount of water as a pipe with an internal diameter 6cm, find  $B$ .

$B =$

若  $B$  条内直径为  $A$  厘米的圆形水管的输水量与一内直径为 6 厘米的圆形水管相等，求  $B$ 。

- (iii) If  $C$  is the area of the triangle formed by  $x$ -axis,  $y$ -axis and the line  $Bx + 9y = 18$ , find  $C$ .

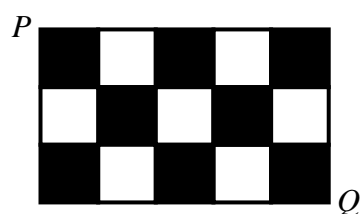
$C =$

若一个由  $x$  轴、 $y$  轴及直线  $Bx + 9y = 18$  所围成之三角形之面积为  $C$ ，求  $C$ 。

- (iv) Fifteen square tiles with side  $10C$  units long are arranged as shown.

$D =$

十五块边长为  $10C$  单位的正方形砖如图排列。



An ant walks along the edges of the tiles, always keeping a black tile on its left. Find the shortest distance  $D$  that the ant would walk in going from  $P$  to  $Q$ .

一蚁沿砖之边缘爬行，而其左边必为一黑砖。求  $D$ ，此蚁由  $P$  爬至  $Q$  之最短距离。